

## Dimensioning and Modeling of a Circular Inductor Integrated in a Boost Converter

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This paper presents the dimensioning and modeling of a circular inductor integrated in a Boost micro converter. At first, we define the characteristics of the Boost micro converter, which is the starting point for the design our component, taking into account the electrical and magnetic characteristics of the materials selected. The second, a Boost micro converter schematic simulation coupled with ideal and integrated inductor was presented. This conceptual model of the Boost is best understood in terms of the relation between voltage and current of the inductor. Finally, we have simulated the electromagnetic effects in integrated inductor in the air, and with substrate using the finite element method.

**Keywords:** Circular inductor integrated, Boost converter, Electromagnetic, Finite element method.

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### 1. INTRODUCTION

The dimensioning and modeling of the integrated component knows a renewed interest because even the density of components on substrates whose dimensions have experienced a reverse progression [1]. In this regard, several studies were conducted [2], first by the development of a design, modeling and the simulation of a square planar micro-transformer [3], the study and modeling of the micro coil using the finite element method [4] and finally the design and modeling of inductor integrated in a Buck micro converter [5]. The aim of our work is a dimensioning a circular inductor that will be integrated in a Boost micro converter. We have implemented the literature processes for the design of our inductor and calculation of geometry parameters characterizing our component. We have also developed the electromagnetic model using the finite element method.

### 2. PRESENTATION OF THE BOOST MICRO-CONVERTER

We have chosen a Boost micro converter (Fig. 1). The inductor to integrate will thus be dimensioned for this type of application. Input voltage,  $V_{in} = 2.5$  Volt. Output voltage,  $V_{out} = 5$  Volt. Maximum current  $I_{Lmax} = 2A$ . Output power,  $P_{out} = 4$  W. Frequency of operation,  $f = 1$  MHz.

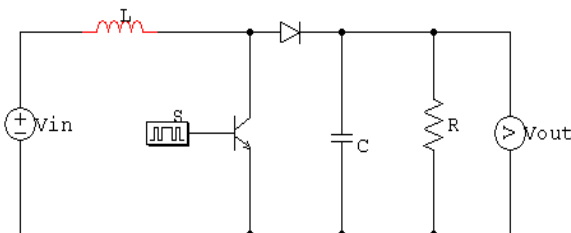


Fig. 1 – Boost converter

The average output current  $I_{out}$  is calculated by formula (1)

$$I_{out} = \frac{P_{out}}{V_{out}} \quad (1)$$

The current through the inductor is calculated by formula (2)

$$I_{Lmin} = 2I_{out} - I_{Lmax} \quad (2)$$

The average current  $I_L$  is expressed as follows (3)

$$I_L = I_{Lmax} + I_{Lmin} \quad (3)$$

We can calculate the value of the inductance L according to relation (4)

$$L = \frac{\alpha \cdot (1 - \alpha) \cdot V_{out}}{I_L \cdot f} \quad (4)$$

Where,

$$\alpha = 1 - (V_{in} / V_{out}) \quad (5)$$

The maximum energy stored in the inductor is given by relation (6)

$$W = \frac{1}{2} L I_{out}^2 \quad (6)$$

The volumetric energy density of the ferrite is given by the equation (7)

$$W_{vmax} = \frac{B_{max}^2}{2\mu_0\mu_r} \quad (7)$$

$B_{max}$ : The maximum magnetic induction supported by the ferrite

$\mu_r$ : The relative permeability

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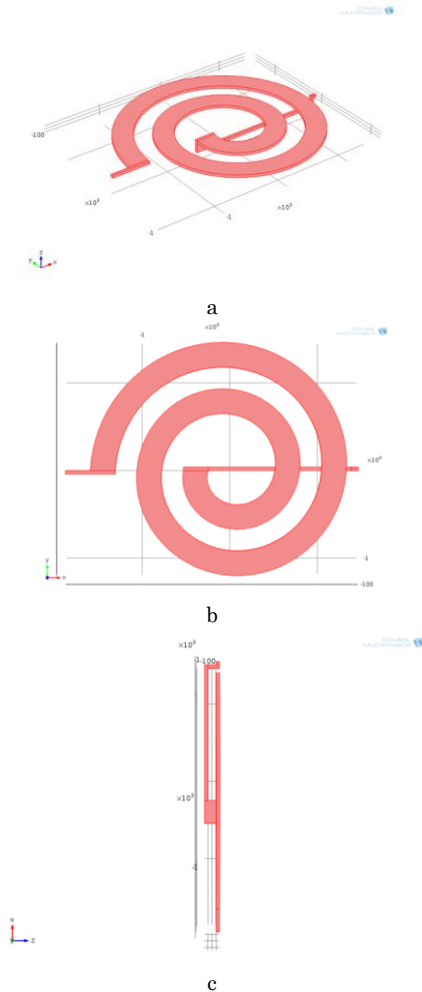
$\mu_0$  : The magnetic permeability of the free space  
The volume of the ferrite is given by relation (8)

$$Vol = \frac{W}{W_{vmax}} \quad (8)$$

The ferrite's thickness is  $t_{Sub} = 96 \mu m$ , thus the volume will be  $3100 \times 3100 \times 96 \mu m^3$ .

### 3. DIMENSIONING OF INTEGRATED CIRCULAR INDUCTOR

The geometry parameters characterizing the integrated inductor (Fig. 2) are the number of turns  $n$ , the width of the conductor  $w$ , thickness of the conductor  $t$ , the spacing between conductor  $s$ , length of the conductor  $l$ , the outer diameter  $d_{out}$  and input diameter  $d_{in}$  [6].



**Fig. 2** – Geometry of integrated circular spiral inductor, (a) general view, (b) view dessus, (c) front view

We find in the literature several formulas which allow us to calculate the number of turns  $n$  according to the value of inductance  $L$ , we chose the Mohan's formula (9). The coefficients  $C_1, C_2, C_3$  and  $C_4$  are defined for each geometry. For a circular inductor spiral,  $C_1 = 1, C_2 = 2.46, C_3 = 0$  and  $C_4 = 0.2$  [7].

$$L = \frac{\mu_0 n^2 d_{avg} C_1}{2} \left\{ \ln\left(\frac{C_2}{\rho}\right) + C_3 \rho + C_4 \rho^2 \right\} \quad (9)$$

Where, we define the average diameter as  $d_{avg} = (d_{out} + d_{in}) / 2$  [8].  $A_m$  the factor's form defined as  $A_m = d_{out} - d_{in} / d_{out} + d_{in}$ .

The spacing between conductors is expressed as follows (10)

$$s = \frac{d_{out} + d_{in} - 2wn}{2(n-1)} \quad (10)$$

The length of the trace is expressed as follows (11)

$$l = \pi i.n.d_{avg} \quad (11)$$

The skin thickness is defined as (12)

$$\delta = \sqrt{\frac{\rho}{\pi \mu f}} \quad (12)$$

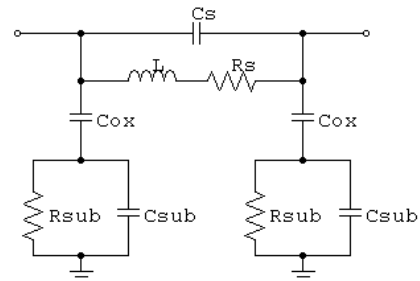
Where  $\rho$  represent the resistivity of the conductor,  $\rho_{Copper} = 1.7 \cdot 10^{-8} \Omega \cdot m$  and  $\mu$  its magnetic permeability. So that the current flows in the entire conductor, it is necessary that one of the following conditions is filled,  $w \leq 2\delta$  or  $t \leq 2\delta$ . Table 1 contains the specifications and the design results of the circular spiral integrated inductor.

**Table 1** – Design results of the circular spiral integrated inductor

Parameter	Value
Inductance, $L$ ( $\mu H$ )	0.5
External diameter, $d_{out}$ (mm)	3
Internal diameter, $d_{in}$ (mm)	0.9
Number of turns, $n$	2
Thickness of the conductor, $t$ ( $\mu m$ )	40
Width of the conductor, $w$ ( $\mu m$ )	280
Spacing between conductor, $s$ ( $\mu m$ )	245
Length of the conductor, $l$ (mm)	15.9

### 4. ELECTRICAL MODEL

The equivalent electrical model of the integrated inductor [9-10] is shown in Fig. 3.



**Fig. 3** – Equivalent electrical model

The series resistance  $R_s$ , can be approximated as (13)

$$R_s = \frac{\rho l}{wt} \quad (13)$$

The parasitic capacitance can be modeled as  $C_s$  (14)

$$C_s = tl \frac{\epsilon_0 l}{s} \quad (14)$$

Where,  $\epsilon_0$  is the permittivity of free space,  $\epsilon_0 = 8.854187 \cdot 10^{-12} \text{Mm}^{-1}$ .

The substrate capacitance  $C_{sub}$  and resistance  $R_{sub}$  are approximately proportional to the area occupied by the integrated inductor and can be expressed as (15), (16).

$$C_{sub} = \frac{1}{2} \epsilon_0 \epsilon_r \frac{lw}{t_{sub}} \quad (15)$$

$$R_{sub} = 2\rho_{sub} \frac{t_{sub}}{lw} \quad (16)$$

Cox oxide capacitance  $\text{SiO}_2$  can be expressed as (17)

$$C_{ox} = lw \left( \frac{\epsilon_0 \epsilon_{ox}}{t_{ox}} \right) \quad (17)$$

Where  $\epsilon_r, \rho_{sub}$  represent respectively the relative permittivity and the resistivity of substrate and  $t_{ox}$  the oxide thickness. In our case,  $\epsilon_r = 10$ ,  $\rho_{sub} = 45 \cdot 10^{-6} \Omega\text{m}$  and  $t_{ox} = 140\mu\text{m}$ .

The efficiency of integrated inductor is calculated [11-13] according by relation (18)

$$Q = 2\pi \frac{\text{stocked energy}}{\text{dissipated energy}} \quad (18)$$

Table 2 presents electrical parameters of the integrated circular spiral inductor.

**Table 2** – Electricals parameters of the integrated circular spiral inductor

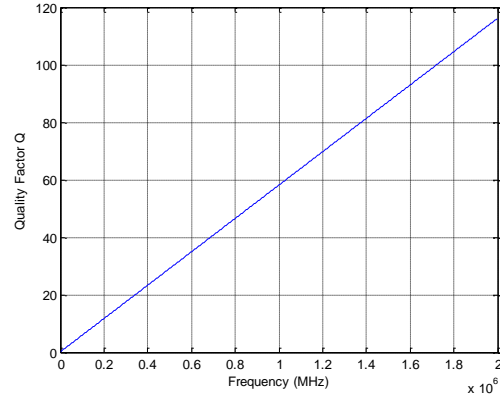
Electricals parameters	Values
$R_s (\Omega)$	0.0241
$R_{sub} (\Omega)$	0.002
$C_s (pF)$	0.023
$C_{ox} (pF)$	15.37
$C_{sub} (pF)$	2.03
$Q$	58

Fig. 4 shows the shape of the quality factor as a function of frequency.

### 5. SIMULATION OF THE OF THE BOOST MICRO CONVERTER

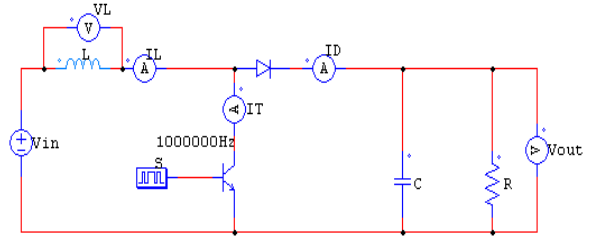
In this simulation, the circuit of Fig. 6 contains an ideal inductor and the Fig. 7 shows the waveform of the output voltage and current of the Boost micro converter. The basic principle of a Boost converter consists of two distinct states (Fig. 5, Fig. 6):

- in the On-state, resulting in an increase in the inductor current;

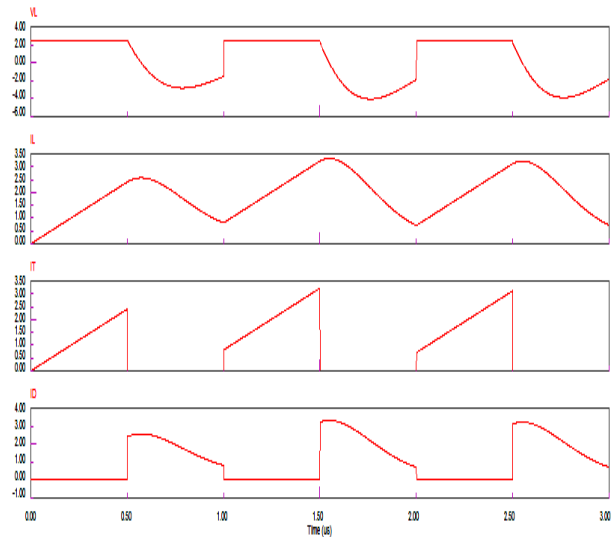


**Fig. 4** – Quality factor  $Q$  from integrated inductor

- in the Off-state, the only path offered to inductor current is through the diode  $D$ , the capacitor  $C$  and the load  $R$ . This result in transferring the energy accumulated during the On-state into the capacitor. The current through the inductor ( $I_L$ ) never falls to zero.



**Fig. 5** – Schematic of boost micro converter coupled with ideal inductor



**Fig. 6** – Waveforms of voltage and current of boost micro converter coupled with ideal inductor

Fig. 7 shows the schematic of micro converter simulated with integrated inductor. The simulated results are indicated in Fig. 8. We observe the same result with ideal and reel inductor.

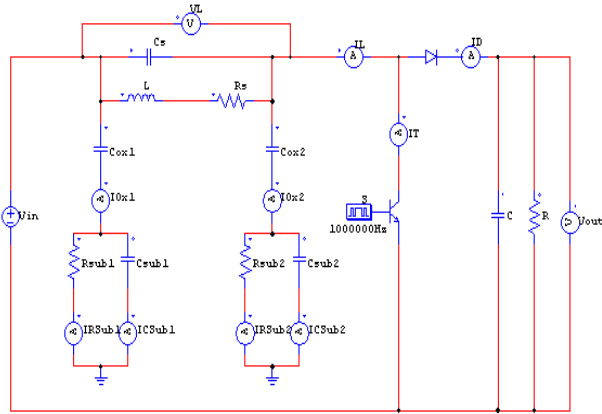


Fig. 7 – Schematic of boost micro converter coupled with integrated inductor

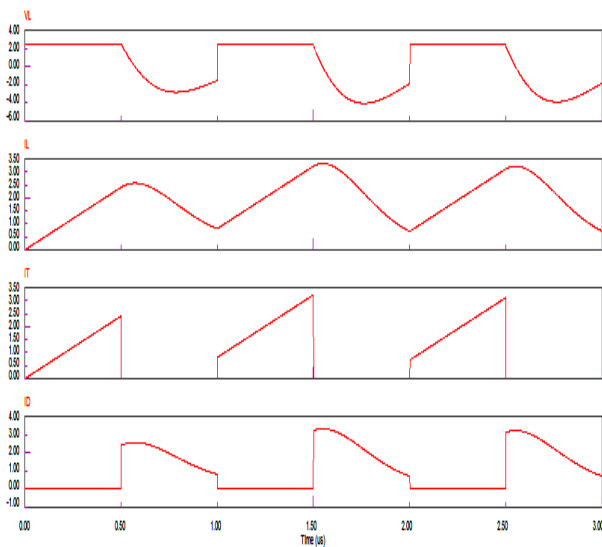


Fig. 8 – Waveforms of voltage and current of boost micro converter coupled with integrated inductor

The results we obtained (Fig. 7, Fig. 9) were compared with those from the literature [14]. We notice the same evolutions therefore quite acceptable and in very good agreement.

### 6. ELECTROMAGNETIC EFFECT OF A CIRCULAR INDUCTOR

In this section, we present the distribution of the electromagnetic field in an inductor in the air and on substrate using finite elements method.

The electric characteristics of materials are shown in Table 3.

Table 3 – Electrics characteristics of the materials

Element	Material	Characteristics
Conductor	Copper (Cu)	Electrical conductivity: $\sigma = 5.998\ 107\ \Omega^{-1}\ m^{-1}$ Relative permeability: $\mu_r = 1$ Relative permittivity: $\epsilon_r = 1$

Substrate	Ferrite (NiFe)	Electrical conductivity: $\sigma = 2.2\ 104\ \Omega^{-1}\ m^{-1}$ Relative permeability: $\mu_r = 800$ Relative permittivity: $\epsilon_r = 10$
Oxide	Silicon dioxide (SiO2)	Electrical conductivity: $\sigma = 1\ \Omega^{-1}\ m^{-1}$ Relative permeability: $\mu_r = 3.9$ Relative permittivity: $\epsilon_r = 1$
Dielectric	Air	Electrical conductivity: : $\sigma = 1\ \Omega^{-1}\ m^{-1}$ Relative permeability: $\mu_r = 1$ Relative permittivity: $\epsilon_r = 1$

In Fig. 9, we observe 3D mesh of integrated inductor in the air.

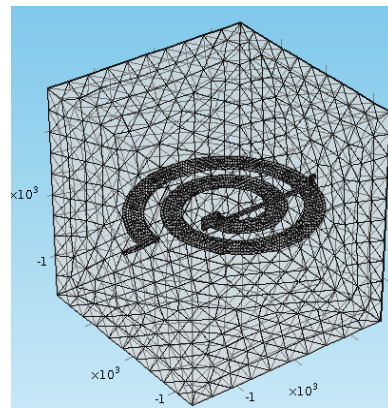
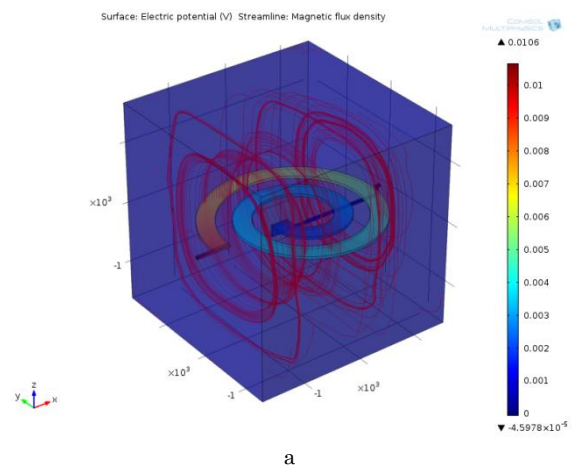
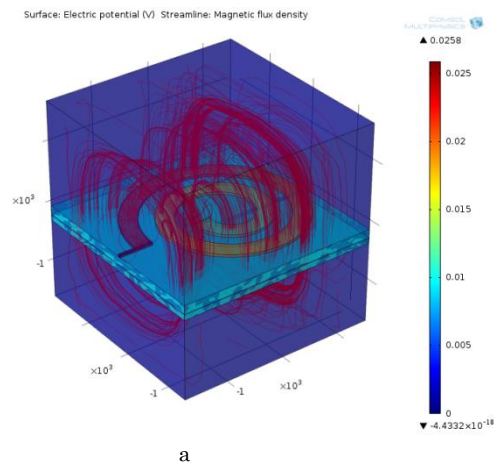
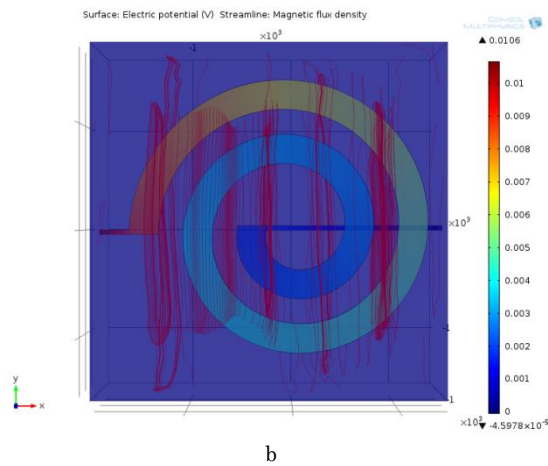


Fig. 9 – 3D mesh of inductor in the air

Fig. 10 shows the distribution of the electric field and magnetic field lines in the inductor in the air.

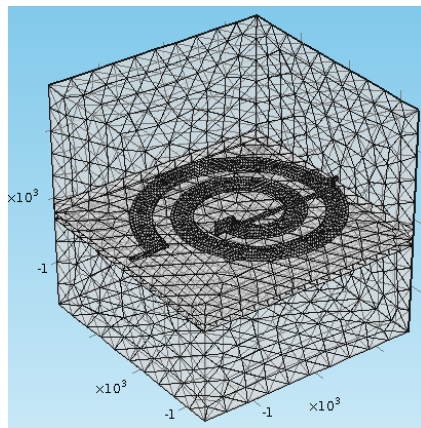
This electric field is important to the input of the component. The magnetic flux density lines are concentrated around the component and are bounded by the borders. The results we obtained (Fig. 10) were compared with those from the literature [15]. We notice the same distributions therefore quite acceptable and in very good agreement.





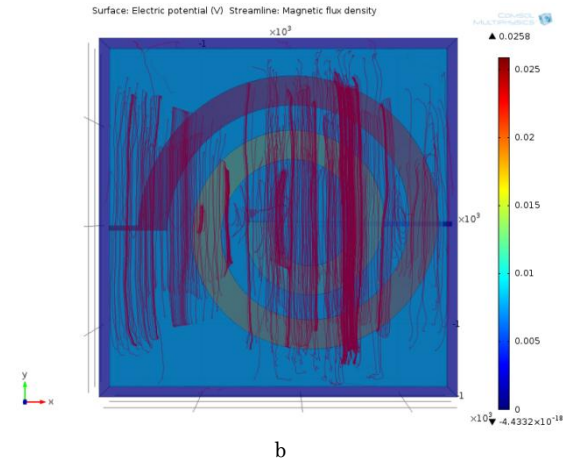
**Fig. 10** – Distribution of magnetic field lines in the inductor in the air, (a) general view

In Fig. 11, we observe 3D mesh of integrated inductor on substrate.



**Fig. 11** – 3D mesh of inductor on substrate

Fig. 12 shows the distribution of the electric field and the magnetic field lines in the inductor on substrate. Still, the electric field is maximum at the input of the integrated inductor. The magnetic field lines are concentrated in the magnetic core, the ferrite (NiFe) which limits the disruption of our component. The results we obtained (Fig. 12) were compared with those from the literature [16]. We notice the same distributions therefore quite acceptable and in very good agreement.



**Fig. 12** – Distribution of magnetic field lines in the inductor on substrate, (a) general view, (b) view dessus

## 7. CONCLUSION

In this paper we addressed the dimensioning and modeling of a circular inductor integrated in a boost converter. We have implemented the literature methods for the design and dimensioning of our integrated inductor, based on the finite element method. We have visualized the electromagnetic phenomenon in inductor in the air and on substrate. We conclude that when we insert a substrate, the majority of the magnetic field lines are concentrated at the walls of the magnetic block. So, the substrate layer is required to have a good electromagnetic compatibility in the case of the integration inductor.

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